

M.Sc (Mathematics/Applied Mathematics)

This is a two year programme. A student has to study 5 courses each year. If one wants to get M.Sc(Mathematics), one must study the following Courses numbered 1 to 7 and and three optional out of the four courses numbered 10A,11A,12A and 13A. If one wants to get M.Sc(Applied Mathematics), one has to study the courses No.1 to 7 and the the three optional courses no. 8B,9B,and 10B.

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